

# Network Legos: Building Blocks of Cellular Wiring Diagrams

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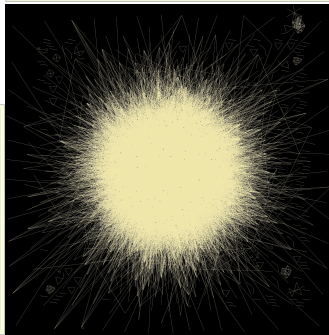
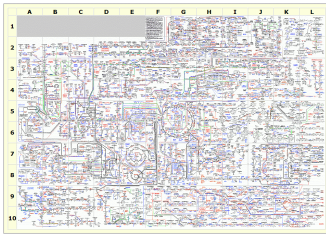
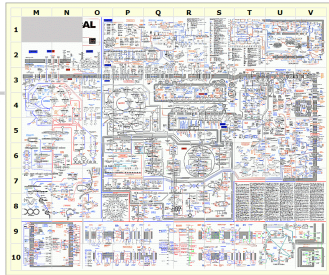
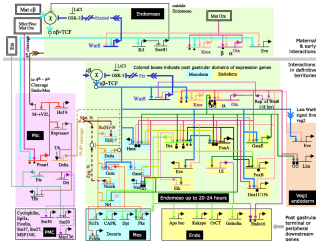
# Goals of Systems Biology

- ▶ Identify the building blocks of molecular interaction networks
- ▶ Interconnect the building blocks to build high level models of the cell
- ▶ Understand the interaction of the building blocks over time and under different conditions

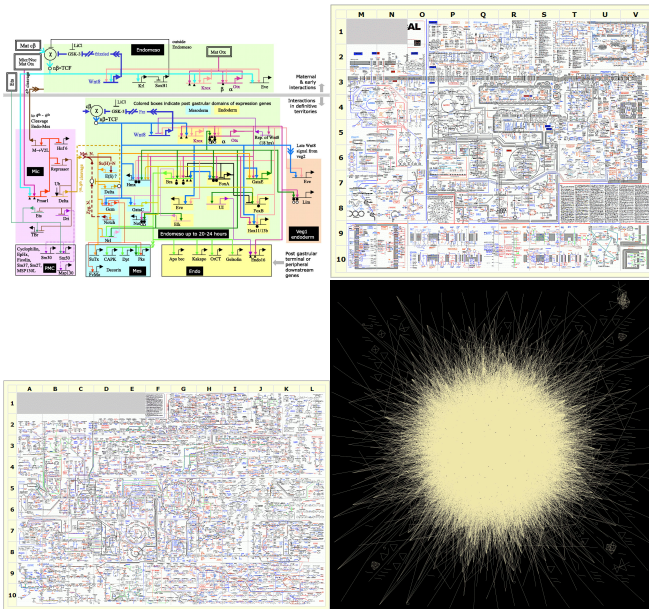
# Goals of Systems Biology

- ▶ Identify the building blocks of molecular interaction networks
- ▶ Interconnect the building blocks to build high level models of the cell
- ▶ Understand the interaction of the building blocks over time and under different conditions
- ▶ How do we automatically construct these building blocks?

# Cellular Wiring Diagrams



# Cellular Wiring Diagrams



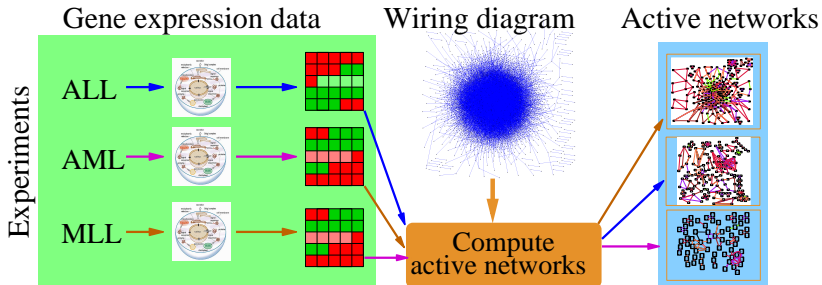
► These wiring diagrams are static.

# Cell State is Dynamic

- ▶ Active molecular interactions change with time, external signals, and perturbations.
- ▶ We need to integrate wiring diagram with other types of data to compute the cell's response to different conditions.

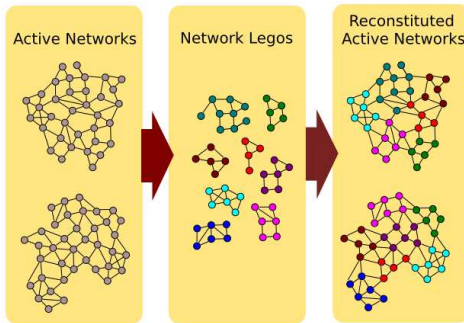
# Active Networks

- ▶ Transcriptional regulatory measurements provide dynamic snapshots of cellular activity.
- ▶ *Active networks*: Molecular interactions activated by the cell in response to a stimulus.
- ▶ Methods to integrate wiring diagram with transcriptional measurements to compute response networks:
  - ▶ Ideker et al., Bioinformatics 2002
  - ▶ Luscombe et al., Nature 2004
  - ▶ Han et al., Nature 2004
  - ▶ Ulitsky and Shamir, BMC Sys Bio 2007



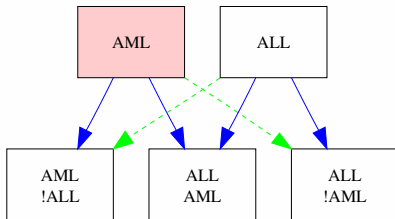
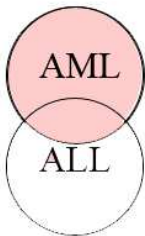
# Goals of the Network Lego Approach

- ▶ What are the similarities and differences between active networks?
- ▶ Can we identify building blocks or network legos that constitute each of the active networks?



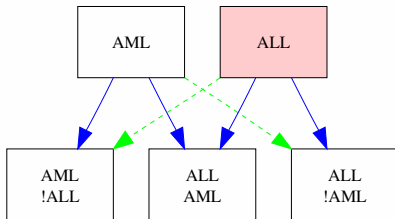
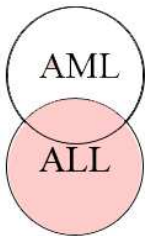


# Comparing Two Active Networks



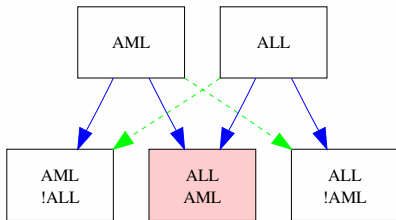
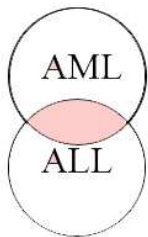
AML

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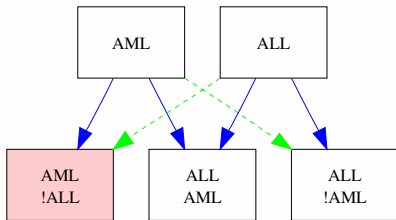
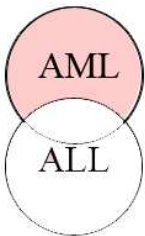
ALL

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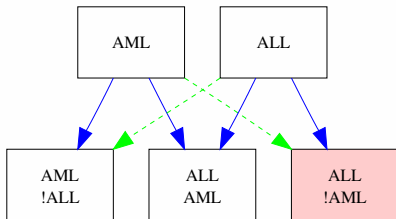
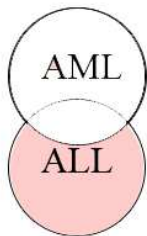
$AML \cap ALL$

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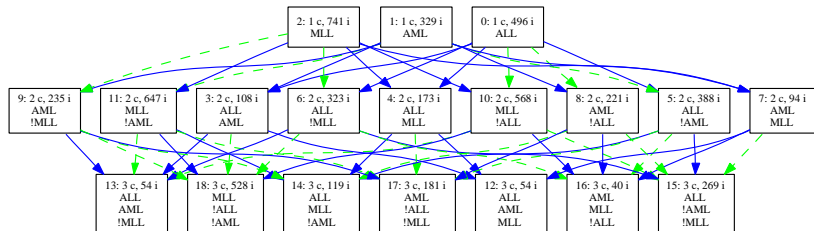
$AML \cap !ALL$

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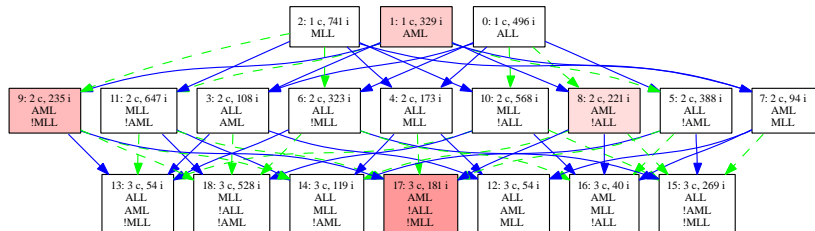


$ALL \cap !AML$

# Comparing Three Active Networks

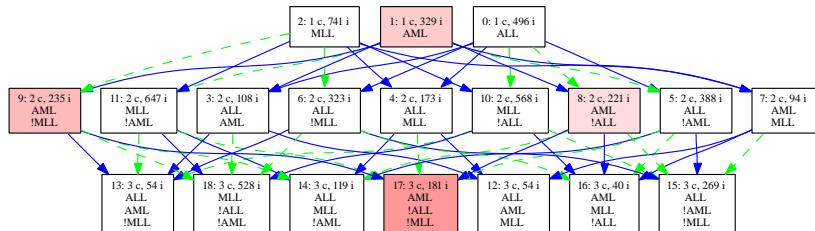


# Differential Activation of the Kit Receptor Pathway in AML



- ▶ AML: p-value  $2 \times 10^{-4}$
- ▶ AML  $\cap$  !ALL: p-value  $1 \times 10^{-3}$
- ▶ AML  $\cap$  !MLL: p-value  $6.7 \times 10^{-5}$
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# Differential Activation of the Kit Receptor Pathway in AML



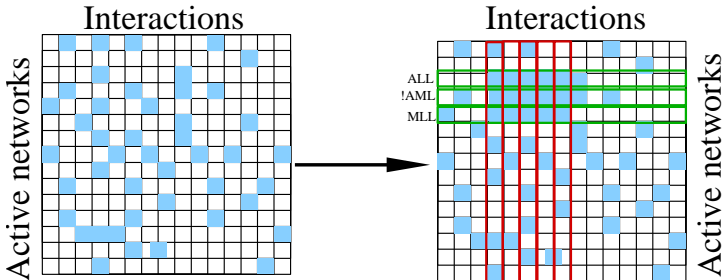
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- ▶ AML  $\cap$  !ALL  $\cap$  !MLL: p-value  $3.5 \times 10^{-7}$
- ▶ c-KIT receptor is activated in almost all subtypes of AML but not in ALL (Reuss-Borst et al., *Leukemia*, 1994, Bene et al., *Blood*, 1998, Schwartz et al., *Leuk Lymphoma.*, 1999).



# Challenges in Comparing Arbitrary Numbers of Active Networks

- ▶ How to do we efficiently compute all combinations?
- ▶ Which combinations are the network legos?
- ▶ How do we demonstrate that we have found network legos?

# How to do we efficiently compute all combinations?

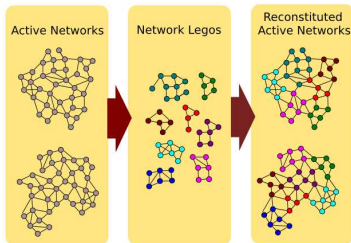


- ▶ Construct a binary matrix  $M$  whose columns are interactions.
- ▶ Represent each active network and its complement in  $M$ 's rows.
- ▶ Compute all closed biclusters in  $M$ .
- ▶ Connect biclusters in a DAG.

# Which combinations are the network legos?

- ▶ For each bicluster  $B$  with  $n$  non-complemented and  $c$  complemented active networks
  1. Pick  $n$  non-complemented and  $c$  complemented active networks repeatedly at random, compute the number of interactions induced by this combination, and build a distribution of the number of interactions.
  2. Set the  $p$ -value of  $B$  to be the fraction of random biclusters with more interactions than  $B$ .
- ▶  $B$  is a *network lego* if it is more significant than any of its ancestors or descendants in the DAG.

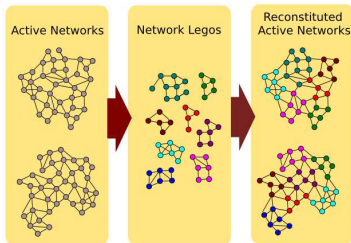
# How do we demonstrate that we have found network legos?



## ► Stability

- Sequentially remove each active network from the input and recompute network legos.
- For each original network lego, compute the fraction of leave one out datasets for which the network lego occurs with at least 95% fidelity.

# How do we demonstrate that we have found network legos?



## ▶ Stability

- ▶ Sequentially remove each active network from the input and recompute network legos.
- ▶ For each original network lego, compute the fraction of leave one out datasets for which the network lego occurs with at least 95% fidelity.

## ▶ Recoverability

- ▶ Compute the union of network legos.
- ▶ Measure the size of the intersection of each active network with this union.

# Analysis of Human Stress Data

- ▶ 13 distinct stresses applied to human cells (Murray et al., Mol. Bio. Cell, 2004).
- ▶ Stress conditions include heat shock, oxidative stress, cell cycle arrest, and crowding.
- ▶ Two cell types: WI38 Fibroblasts and Hela.
- ▶ Murray et al. note that each stress elucidated a unique response.

# Human Stress Results

- ▶ 13 stresses and their active networks yielded 444201 closed biclusters.
- ▶ 143 biclusters are network legos.
- ▶ The network legos contained between 165 and 1148 proteins.
- ▶ The network legos have 95% stability.
- ▶ The network legos provide better than 86% recoverability for all active networks.
- ▶ We recovered 11 active networks at 100%.

|             |   |   |    |    |    |    |    |    |
|-------------|---|---|----|----|----|----|----|----|
| #conditions | 5 | 6 | 7  | 8  | 9  | 10 | 11 | 12 |
| #legos      | 1 | 6 | 10 | 36 | 34 | 20 | 28 | 8  |

# Human Stress Results without Cell Cycle Arrest Treatment

- ▶ The response networks for cell cycle arrest treatments contain interactions that are distinct compared to the interaction from other treatments.
- ▶ 11 stresses yielded only 15 network legos.
- ▶ The network legos provide better than 71% recoverability for all active networks.
- ▶ We recovered five active networks at 100%.
- ▶ Each formula contained at least 7 active networks



# WI38 Menadione and WI38 DTT Network Lego

- ▶ One network lego contained endoplasmic reticulum stress and oxidative stress to fibroblasts in non-complemented form.
- ▶ All other stresses appeared in complemented form.
- ▶ This network lego is the only one enriched in functions related to the cell cycle and targets of the E2F1 transcription factor.
- ▶ Fibroblasts respond differently from HeLa cells to these two stresses.

# Our Contributions

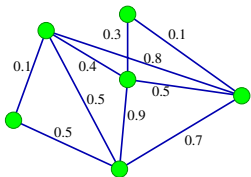
- ▶ Combined representation of biological processes using formulae and network legos.
- ▶ A formula relates different cellular states or perturbations by explicitly denoting their participation via intersections and complements.
- ▶ Each network lego corresponds to a functional module of coherently interacting genes in the universal network.
- ▶ Network legos serve as building blocks of active networks.

# Future Work

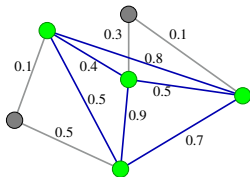
- ▶ Explore network legos in the context of a larger compendium of cellular stresses.
- ▶ Develop an algorithm to directly compute network legos without searching the space of all active network combinations.
- ▶ Determine rules and grammar for combining network legos into active networks.

# Algorithmic Ingredients: Active Networks

(i) Assign Pearson's correlation as the interaction weight



(ii) Compute dense subgraphs



- ▶ Compute the Pearson's correlation coefficient of the expression profiles of the interacting genes.
- ▶ Search for pockets of concerted activity using an algorithm for finding dense subgraphs.